## Chapter # 2

## Logarithms

## Exercise # 2.2

Question # 1: Express each of the following in logarithmic form.

(i) 
$$10^3 = 1000$$
  
 $\log_{10} 1000 = 3$  (Ans)

(iv) 
$$20^2 = 400$$
  
 $\log_{20} 400 = 2$  (Ans

(vii) 
$$p = q^r$$
  
 $q^r = p$   
 $\log_q p = r$  (Ans)

(ii) 
$$2^8 = 256$$
  
 $\log_2 256 = 8$  (Ans)

(v) 
$$16^{-\frac{1}{4}} = \frac{1}{2}$$
 $\log_{16} \frac{1}{2} = -\frac{1}{4}$  (Ans)

(viii) 
$$(32)^{\frac{-1}{5}} = \frac{1}{2}$$

$$\log_{32} \frac{1}{2} = \frac{-1}{5} \quad \text{(Ans)}$$

(iii) 
$$3^{-3} = \frac{1}{27}$$
 $\log_3 \frac{1}{27} = -3$  (Ans)

(vi) 
$$11^2 = 121$$
  
 $\log_{11} 121 = 2$  (Ans)

Question # 2: Express each of the following in exponential form.

(i) 
$$\log_5 125 = 3$$
  
 $5^3 = 125$  (Ans)

(iv) 
$$\log_5 5 = 1$$
  
 $5^1 = 5$  (Ans)

(vii) 
$$\mathbf{5} = \mathbf{log_{10}} \, \mathbf{100000}$$
  
 $\mathbf{log_{10}} \, \mathbf{100000} = \mathbf{5}$   
 $\mathbf{10^5} = \mathbf{1000000}$  (Ans)

(ii) 
$$\log_2 16 = 4$$
  
 $2^4 = 16$  (Ans)

(v) 
$$\log_2 \frac{1}{8} = -3$$
  
 $2^{-3} = \frac{1}{2}$  (Ans)

(viii) 
$$\log_4 \frac{1}{16} = -2$$
  
 $4^{-2} = \frac{1}{16}$  (Ans)

(iii) 
$$\log_{23} 1 = 0$$
  
 $23^0 = 1$  (Ans)

(vi) 
$$\frac{1}{2} = \log_9 3$$
  
 $\log_9 3 = \frac{1}{2}$   
 $9^{\frac{1}{2}} = 3$  (Ans)

Question # 3: Find the value of x in each of the following.

(i) 
$$\log_x 64 = 3$$
  
 $x^3 = 64$   
 $x^3 = 4^3$   
 $x = 4$  (Ans)  $\frac{4 + 64}{4 + 16}$   
 $x = 4$  (Ans)

(iv) 
$$\log_{10} x = -3$$
  
 $10^{-3} = x$   
OR,  
 $x = 10^{-3}$   
 $x = \frac{1}{10^{3}}$   
 $x = \frac{1}{1000}$  (Ans)

(ii) 
$$\log_5 1 = x$$
  
 $5^x = 1$   
 $5^x = 5^0$   
 $x = 0$  (Ans)

(v) 
$$\log_4 x = \frac{3}{2}$$
  
 $4^{\frac{3}{2}} = x$   
OR,  
 $x = 4^{\frac{3}{2}}$   
 $x = 2^{2 \times \frac{3}{2}}$   
 $x = 2^3$   
 $x = 8$  (Ans)

(iii) 
$$\log_x 8 = 1$$
  
 $x^1 = 8$   
 $x = 8$  (Ans)

vi) 
$$\log_2 1024 = x$$

$$2^x = 1024$$

$$2^x = 2^{10}$$

$$x = 10 \text{ (Ans)}$$

$$2 \frac{1024}{2}$$

$$2 \frac{512}{2}$$

$$2 \frac{256}{2}$$

$$2 \frac{128}{2}$$

$$2 \frac{64}{2}$$

$$2 \frac{32}{2}$$

$$2 \frac{16}{2}$$

$$2 \frac{8}{2}$$

$$2 \frac{4}{2}$$

$$2 \frac{2}{2}$$