

Step Academy official

Model Town Grw PH: 03016652757

STUDENT NAME	
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TIME ALLOWED	180
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CLASS	New 1st Year (FSC/ICS)
SUBJECT	Mathematics
TOTAL MARKS	100
Paper Type	

Q1. Choose the correct answer.

20X1=20

1. Complex cube of -1 are:

- (A) ω, ω^2 (B) $1, \omega, \omega^2$ (C) $-1, -\omega, -\omega^2$ (D) $-\omega, -\omega^2$

2. If ω is complex cube root of unity then $\omega = \dots$:

- (A) 0 (B) 1 (C) ω^2 (D) $\frac{1}{\omega^2}$

3. If $f: A \rightarrow B$ is a function such that $\text{rang } f \subset B$, then f is called a/an function:

- (A) Onto (B) Injective (C) Bijective (D) Into

4. One root of equation $x^2 - 3x + a = 0$ is 2, then a is:

- (A) -2 (B) 2 (C) 3 (D) -3

5. An equation involving radical expression of the variable is called

- (A) Radical equation (B) Algebraic equation (C) Exponential equation (D) None of these

6. Graph of quadratic equation will be:

- (A) Straight line (B) Curve (C) Set of line (D) None

7. If A is non-singular square matrix, then AA^{-1} equals

- (A) A (B) A^{-1} (C) 0 (D) 1

8. A relation in which the equality is true for all finite values of unknowns is called an

- (A) Identity (B) Improper fraction (C) Proper fraction (D) Equation

9. $\frac{P(x)}{x^2 + 1}$ will be proper fraction if degree of $P(x)$ equals:

- (A) 1 (B) 2 (C) 3 (D) 0

10. If the n th term of an A.P is $\frac{1}{2}(3-n)$, then first three terms are:

- (A) 3, 2, 1 (B) 1, 2, 3 (C) 1, 2, 1 (D) 1, 1/2, 0

11. If $a_n = (-1)^{n+1}$ then 26th term is:

- (A) 1 (B) -1 (C) 26 (D) 24

12. If $\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$ are in A.P then the common difference is

- (A) $\frac{2ac}{a-c}$ (B) $\frac{2ac}{a+c}$ (C) $\frac{a-c}{2ac}$ (D) $\frac{a+c}{2ac}$

13. If $a_n = 2n - 5$, then 7th term is:

- (A) 9 (B) 15 (C) 11 (D) 13

14. The nth term of an A.P is $\frac{1}{2}(3n)$ the first three terms are

- (A) 3,2,1 (B) 1,2,3 (C) $\frac{3}{2}, 3, \frac{9}{2}$ (D) $\frac{3}{2}, 9, \frac{9}{2}$

15. The common ratio a G.P. cannot be

- (A) 3 (B) 1 (C) 2 (D) 0

16. No term of geometric sequence can be:

- (A) 0 (B) 1 (C) 2 (D) 3

17. For an infinite geometric series for which $|r| < 1$, $S_n = ?$ where $N = \infty$:

- (A) $\frac{a_1(1+r)}{1-r}$ (B) $\frac{a_1}{1-r}$ (C) $\frac{a_1}{2r}$ (D) $\frac{a_1}{2-r}$

18. If $y = \frac{2}{3}x + \frac{4}{9}x^2 + \frac{8}{27}x^3 + \dots$ then interval of convergent is

- (A) $0 < x < -\frac{3}{2}$ (B) $-\frac{3}{2} < x < 0$ (C) $\frac{1}{2} < x < -\frac{1}{2}$ (D) $0 < x < \frac{3}{2}$

19. nC_r is valid only if:

- (A) $n \leq r$ (B) $r \leq n$ (C) $r > n$ (D) r

20. In how many ways a cricket team of 11 players out of 15 can be selected if the captain must include in each way:

- (A) $15!$ (B) ${}^{14}C_{10}$ (C) ${}^{15}C_{11}$ (D) $11!$

Q2. write the answers of following questions. Any 8

8X2=16

1. Solve the following complex quadratic equation by completing square method: $z^2 - 6z + 30 = 0$

2. Evaluate: $\left(\frac{-1 + \sqrt{-3}}{2}\right)^7 + \left(\frac{-1 - \sqrt{-3}}{2}\right)^7$

3. Show that: $(1 - \omega + \omega^2)(1 - \omega^2 + \omega^4)(1 - \omega^4 + \omega^8)(1 - \omega^8 + \omega^{16}) \dots$ to $2n$ factors $= 2^{2n}$

4. Plot the following points: (-3, 120)

5. Plot the following points: $\left(-\frac{9}{2}, -\frac{19\pi}{12}\right)$

6. Find $\frac{f(a+h) - f(a)}{h}$ and simplify where: $f(x) = 4x + 7$

7. Given $f(x) = x^3 - 2x^2 + 4x - 1$ find: $f(1)$

8. Graph the following function: $y = -\frac{1}{2}\sqrt{x}$

9.

The value of a stock follows the exponential growth model $P(t) = P_0 e^{rt}$. Where P_0 is the initial stock price, r is the growth rate per year and t is the time in years. Suppose a stock is currently valued at Rs., 5,000 and it is expected to grow at a rate of 5% per year. (i) Find the value of the stock after 10 years. (ii) After many years will the stock double in value?

10 . Find the real values of x and y in the following: $\frac{x}{2+i} + \frac{y}{3-i} = 4 + 5i$

11 . If z_1 and z_2 are two complex numbers, show that: $\text{Arg}(z_1 z_2) = \text{Arg } z_1 + \text{Arg } z_2$

12 . Express the complex number $1 + i\sqrt{3}$ in polar form.

Q4. write the answers of following questions. Any 8

8X2=16

1 . Find the maximum and minimum point by sketching the following quadratic function. Also find their domain and range: $f(x) = -x^2 - 4x + 4$

2 . Solve the following absolute value quadratic equation and inequalities: $|x^2 - 4| < 5$

3 . Solve the following absolute value quadratic equation and inequalities: $|x^2 - 5x + 6| \leq x + 2$

4 . If $A = [a_{ij}]_{3 \times 4}$, then show that, $I_3 A = A$

5 . If A and B are square matrices of the same order, then explain why in general; $(A + B)^2 \neq A^2 + 2AB + B^2$

6 . Without expansion show that: $\begin{vmatrix} -a & 0 & b \\ 0 & a & -c \\ c & -b & 0 \end{vmatrix} = 0$

7 . If A is a square matrix of order 3, then show that $|KA| = K^3 |A|$.

8 . Find the rank of the matrix $\begin{bmatrix} 1 & -1 & 2 & -3 \\ 2 & 0 & 7 & -7 \\ 3 & 1 & 12 & -11 \end{bmatrix}$.

9 . A triangle has $A(2,3)$, $B(-1,4)$ and $C(3,-2)$. Find the vertices of the reflected triangle over the x-axis by using transformation matrix.

10 . Reduce $\begin{bmatrix} 2 & 3 & -1 & 9 \\ 1 & -1 & 2 & -3 \\ 3 & 1 & 3 & 2 \end{bmatrix}$ to (row) echelon and reduce (row) echelon form.

11 . Using properties of determinants, show that: $\begin{vmatrix} a^2 + b^2 & c^2 & c^2 \\ a^2 & b^2 + c^2 & a^2 \\ b^2 & b^2 & c^2 + a^2 \end{vmatrix} = 4a^2 b^2 c^2$

12 . If A and B are two matrices such that $AB = B$ and $BA = A$, show that $A^2 + B^2 = A + B$.

Q5. write the answers of following questions. Any 9

9X2=18

1 . Sum the series: $\frac{4}{\sqrt{5}} + \sqrt{5} + \frac{6}{\sqrt{5}} + a_n$

2 . Find S_n for the following arithmetic series: $a_1=4$, $n=25$, $a_n=100$

3 . If $\frac{1}{a+b}$, $\frac{1}{c+a}$, $\frac{1}{b+c}$ are in A.P then show that a^2, b^2, c^2 are in A.P

4 . Find the first three terms of an arithmetic series in which $a_1=9$, $a_n=105$ and $S_n=741$.

- 5 . If a, b, c, d are in G.P., Prove that: $a-b, b-c, c-d$ are in G.P.
- 6 . Find the eight term of a geometric sequence for which $a_1 = -3$ and $r = -2$.
- 7 . Find the n^{th} term of the G.P., 3, 12, 48,
- 8 . Sum the following series upto n terms: $1 \times 2 + 2 \times 5 + 3 \times 8 + \dots$
- 9 . Evaluate the following: ${}^{50}C_{50}$
- 10 . Find the number of possible arrangements of vowel letters from the English alphabet?
- 11 .
Resolve the following into partial fraction: $\frac{2}{x^2 - 1}$
- 12 . Find the next four terms of the following sequence: 12, 16, 20, ...
- 13 . Find a_{n+1} and a_n if $a_n = 4 + 3n$.

Q. write the answers of following questions. Any 6

3X10=30

- 1a .
If ω is a cube root of unity, prove that $\frac{a\omega^{12} + b\omega^{17} + c\omega^{19}}{a\omega^{14} + b\omega^{22} + c\omega^{30}} = \omega$
- b .
If $z_1 = 9\left(\cos\frac{5\pi}{4} + i\sin\frac{5\pi}{4}\right)$ and $z_2 = 5\left(\cos\frac{\pi}{3} + i\sin\frac{\pi}{3}\right)$ then find: $\frac{z_1}{z_2}$
- 2a .
Find $\frac{f(a+h) - f(a)}{h}$ and simplify where: $f(x) = \sin x$
- b .
Find the point (s) of intersection of the following function graphically: $f(x) = -3x - 4$, $g(x) = \frac{1}{2}x + 3$
- 3a .
Find the maximum and minimum value of the following quadratic function by completing squares: $f(x) = -2x^2 - x + 21$
- b .
Solve the following: $3x^2 + 15x - 2\sqrt{x^2 + 5x + 1} = 2$
- 4a .
Using properties of determinants, show that: $\begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix} = (a+b+c)^3$
- b .
Solve the following systems of linear equation by Cramer's rule: $\left. \begin{array}{l} x_1 + 2x_2 - 3x_3 = 0 \\ 4x_1 - x_2 + x_3 = 5 \\ -2x_1 + 3x_2 + 2x_3 = 3 \end{array} \right\}$
- 5a .
Resolve $\frac{1}{(x+1)^2(x^2-1)}$ into partial fraction.
- b .
Prove that: $\frac{(2n+1)!}{n!} = [1.3.5..(2n-1)(2n+1)]2^n$